

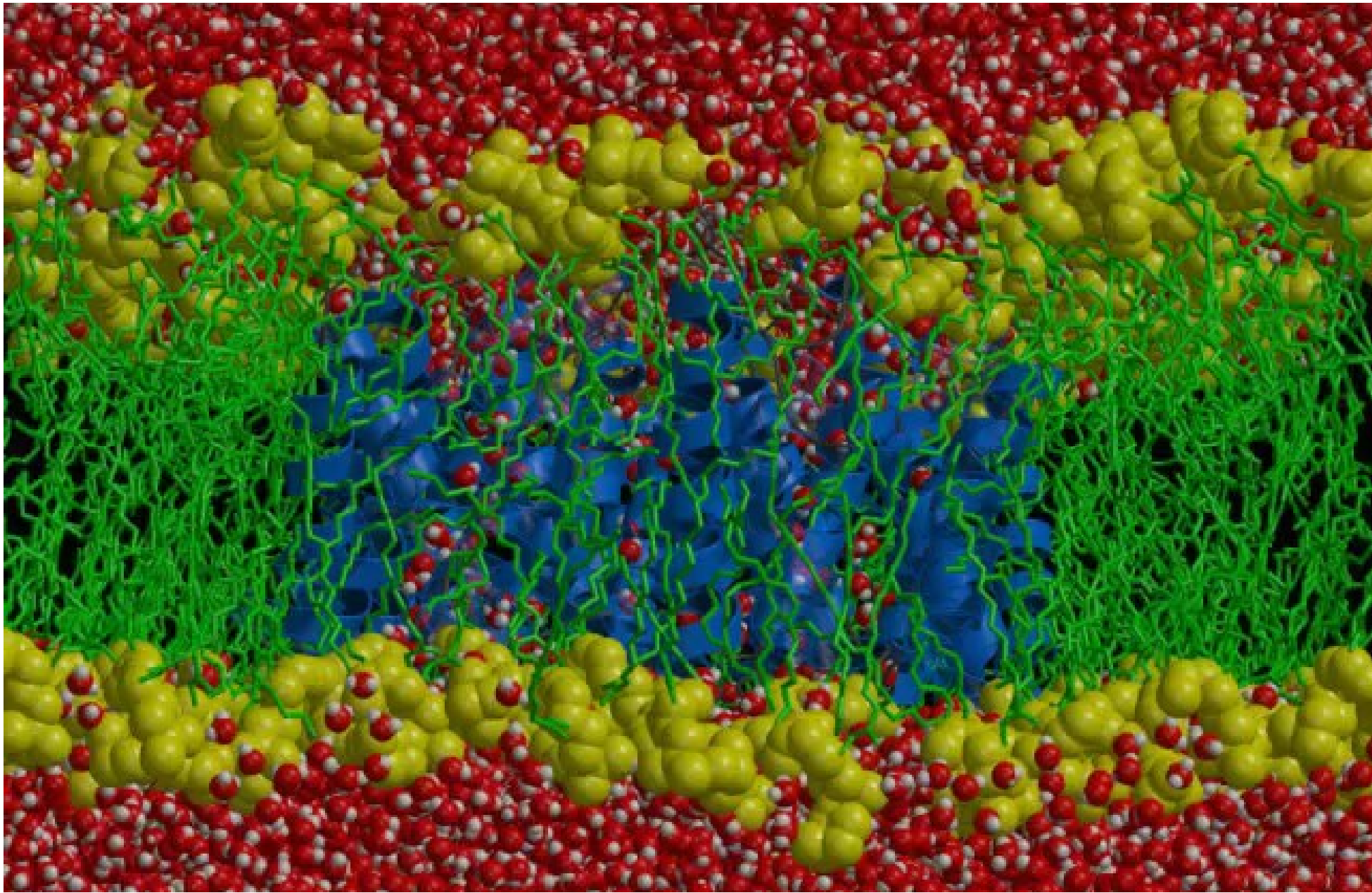
UNIVERSITÄT  
HEIDELBERG



# Simulations

L9 Structural Bioinformatics

WiSe 2023/24, Heidelberg University



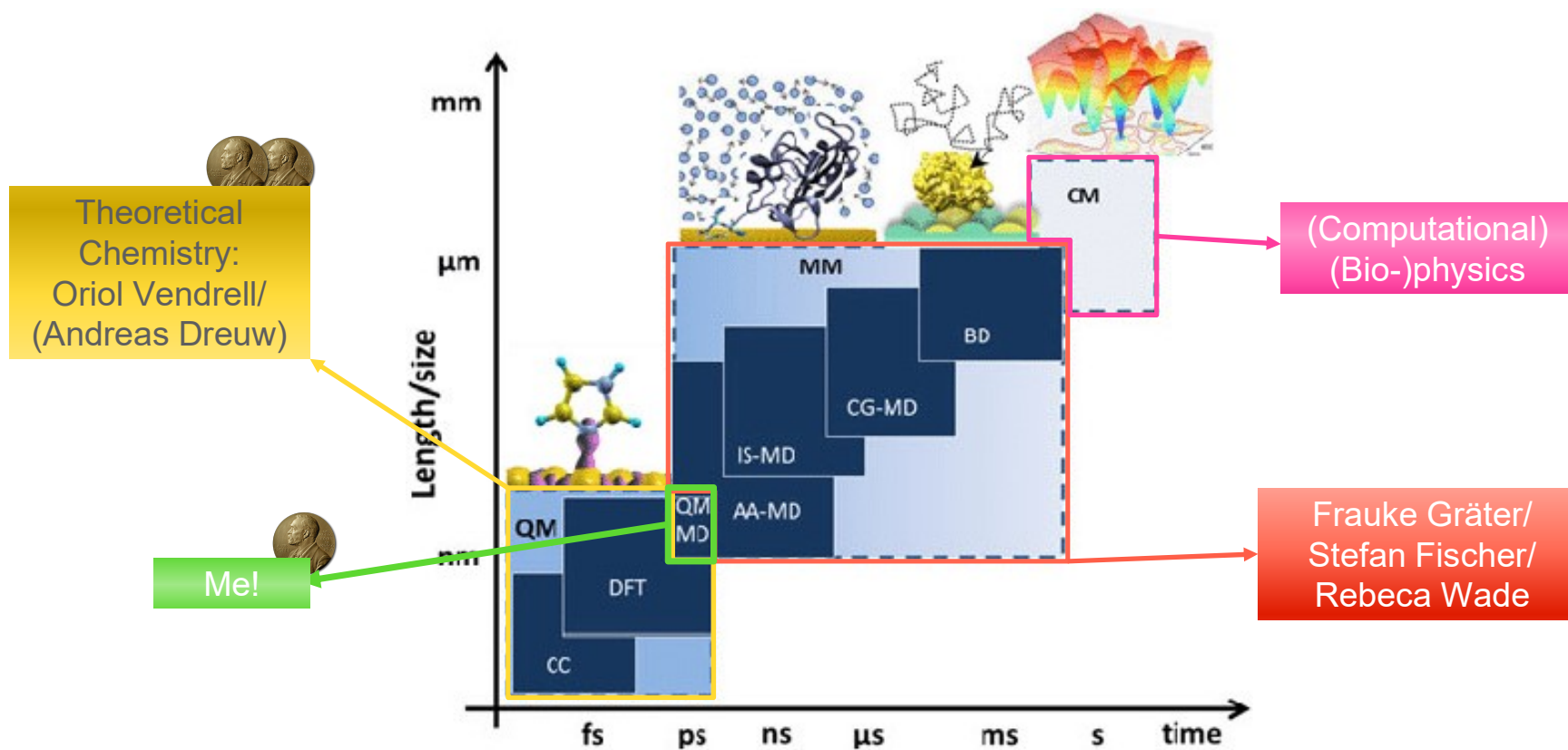
# Outline

1. Overview
2. Approximations
3. Force Fields
4. Algorithms
5. Coarse Grained Simulations
6. Recipe
7. Further Studying

# 1. Overview

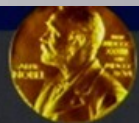
# Overview

## What is possible?



Nobelpriset 2013

The Nobel



# The Nobel Prize in Chemistry 2013



THE ROYAL SW



**Martin Karplus**

Université de Strasbourg,  
France and Harvard  
University, Cambridge,  
MA, USA



**Michael Levitt**

Stanford University School of  
Medicine, CA, USA



**Arieh Warshel**

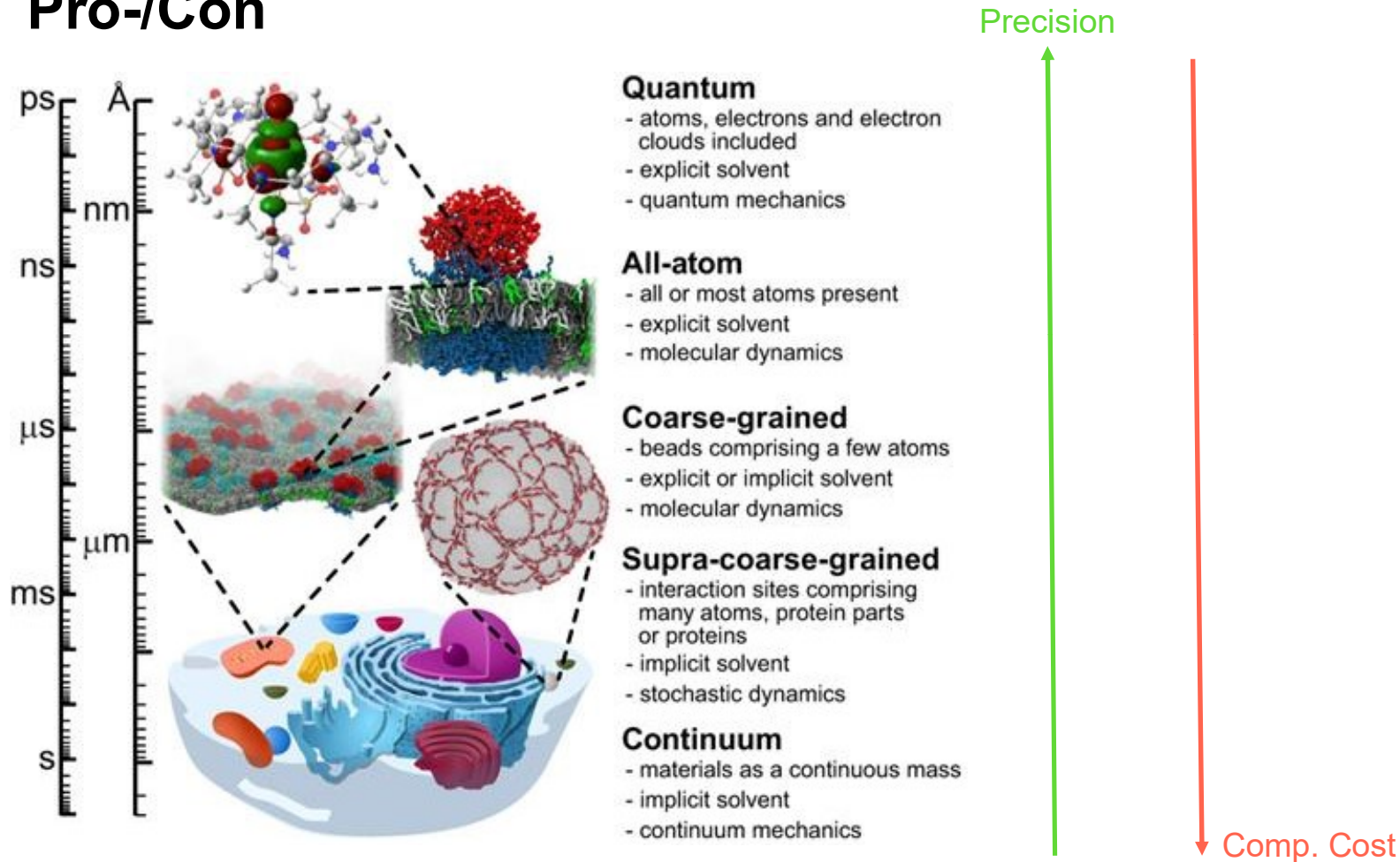
University of Southern  
California, Los Angeles, CA,  
USA

„For the development of multiscale models for complex chemical systems“



# Overview

## Pro-/Con



# 2. Approximations



# Approximations

## Outline



[https://www.chemie-schule.de/KnowHow/Erwin\\_Schr%C3%B6dinger](https://www.chemie-schule.de/KnowHow/Erwin_Schr%C3%B6dinger)

1. Born-Oppenheimer
2. Nuclei move classically
3. Parametrize Force Field

Occasionally  
used in QM

# Approximations

## 1. Born-Oppenheimer

- $m_N \gg m_e$

- $v_N \ll v_e$

# Approximations

## 1. Born-Oppenheimer

$$i\hbar \frac{\partial \Psi(R, r, t)}{\partial t} = -\frac{\hbar^2}{2m} \frac{\partial^2}{\partial r^2} \Psi(R, r, t) - \frac{\hbar^2}{2M} \frac{\partial^2}{\partial R^2} \Psi(R, r, t) + V \Psi(R, r, t)$$

$$\Psi(R, r, t) = \psi(R, t) \phi(r)$$

$$E_e(R) \phi(r) = -\frac{\hbar^2}{2m} \frac{\partial^2}{\partial r^2} \phi(r) + V(R) \phi(r)$$

$$i\hbar \frac{\partial \psi(R)}{\partial t} = -\frac{\hbar^2}{2M} \frac{\partial^2}{\partial R^2} \psi(R, t) + E_e(R) \psi(R, t)$$

# Approximations

## 2. Nuclei move classically

~~$$i\hbar \frac{\partial \psi(R)}{\partial t} = -\frac{\hbar^2}{2M} \frac{\partial^2}{\partial R^2} \psi(R, t) + E_e(R) \psi(R, t)$$~~

$$\frac{\partial^2 R}{\partial t^2} = -\frac{\nabla_R E_e(R)}{M}$$

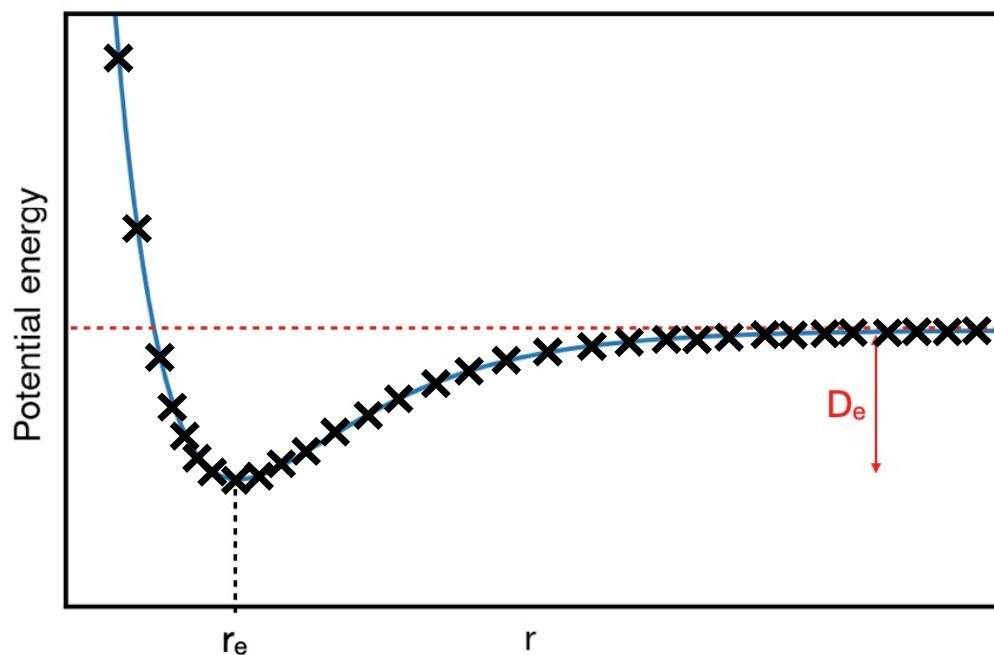
# Approximations

## 2. Nuclei move classically - Breakdowns:

- Tunneling protons
- Vibrational modes

# Approximations

## 3. Parametrize Force Field



**H<sub>2</sub> parameters:**

$$D_e = 4.75 \text{ eV}$$

$$r_e = 0.741 \text{ \AA}$$

$$a = 1.93 \text{ \AA}^{-1}$$

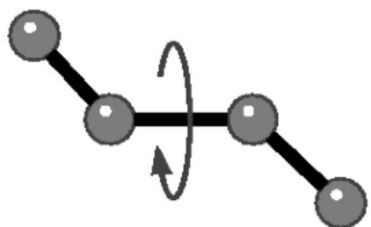
$$V = D_e \left( 1 - e^{-a(r-r_e)} \right)^2$$

# 3. Force Fields



# Force Fields

## Amber



Dihedral angles

$E_{total}$

=

$$\sum_{bonds} k_b (r - r_0)^2$$



Bond length

+

$$\sum_{angles} k_\theta (\theta - \theta_0)^2$$

Bond angle



+

$$\sum_{dihedrals} V_n [1 + \cos(n\phi - \gamma)]$$

Van der Waals forces



+

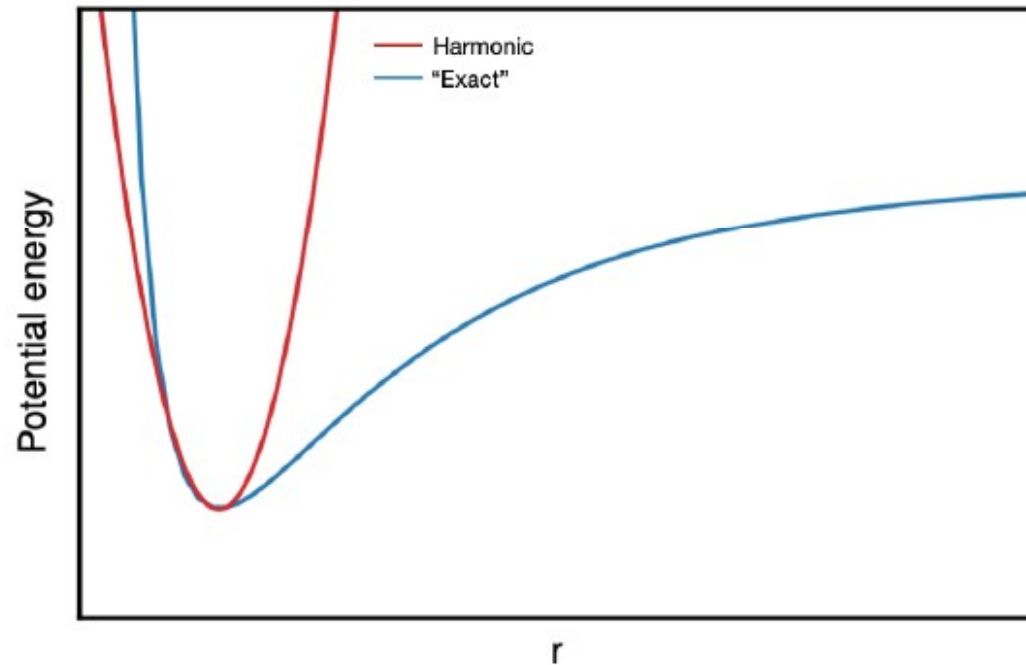
$$\sum_{i=1}^{N-1} \sum_{j=i+1}^N \left[ \frac{A_{ij}}{R_{ij}^{12}} - \frac{B_{ij}}{R_{ij}^6} + \frac{q_i q_j}{\epsilon R_{ij}} \right]$$

Electrostatics



# Force Fields

## Harmonic Approximation



# Force Fields

## Chamber

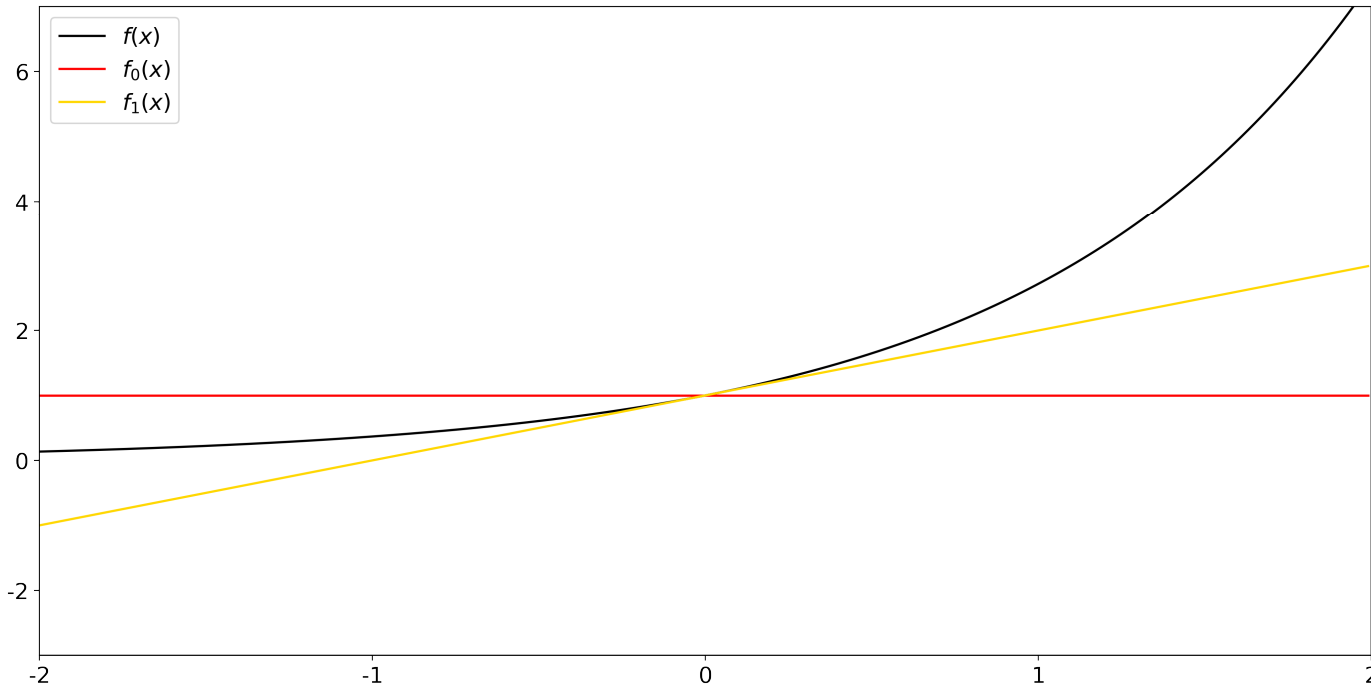
```
ATOMS
MASS 31 H 1.00800 ! polar H
MASS 32 HC 1.00800 ! N-ter H
MASS 33 HA 1.00800 ! nonpolar H
MASS 34 HP 1.00800 ! aromatic H
MASS 35 HB1 1.00800 ! backbone H
MASS 36 HB2 1.00800 ! aliphatic backbone H, to CT2
MASS 37 HR1 1.00800 ! his he1, (+) his HG,HD2
MASS 38 HR2 1.00800 ! (+) his HE1
MASS 39 HR3 1.00800 ! neutral his HG, HD2
MASS 40 HS 1.00800 ! thiol hydrogen
MASS 41 HE1 1.00800 ! for alkene; RHC=CR
MASS 42 HE2 1.00800 ! for alkene; H2C=CR
MASS 43 HA1 1.00800 ! alkane, CH, new LJ params (see toppar_all122_prot_aliphatic_c27.str)
MASS 44 HA2 1.00800 ! alkane, CH2, new LJ params (see toppar_all122_prot_aliphatic_c27.str)
MASS 45 HA3 1.00800 ! alkane, CH3, new LJ params (see toppar_all122_prot_aliphatic_c27.str)
MASS 46 C 12.01100 ! carbonyl C, peptide backbone
MASS 47 CA 12.01100 ! aromatic C
MASS 48 CT 12.01100 ! aliphatic sp3 C, new LJ params, no hydrogens, see retinol stream file for parameters
MASS 49 CT1 12.01100 ! aliphatic sp3 C for CH
MASS 50 CT2 12.01100 ! aliphatic sp3 C for CH2
MASS 51 CT2A 12.01100 ! from CT2 (GLU, HSP chi1/chi2 fitting) 05282010, zhu
MASS 52 CT3 12.01100 ! aliphatic sp3 C for CH3
MASS 53 CPH1 12.01100 ! his CG and CD2 carbons
MASS 54 CPH2 12.01100 ! his CE1 carbon
```

# 4. Algorithms

# Algorithms

## Repetition – Taylor Series

$$f(x) = \sum_{i=0}^{\infty} \frac{f^{(i)}(x_0)}{i!} (x - x_0)^i$$



$$f(x) = e^x$$

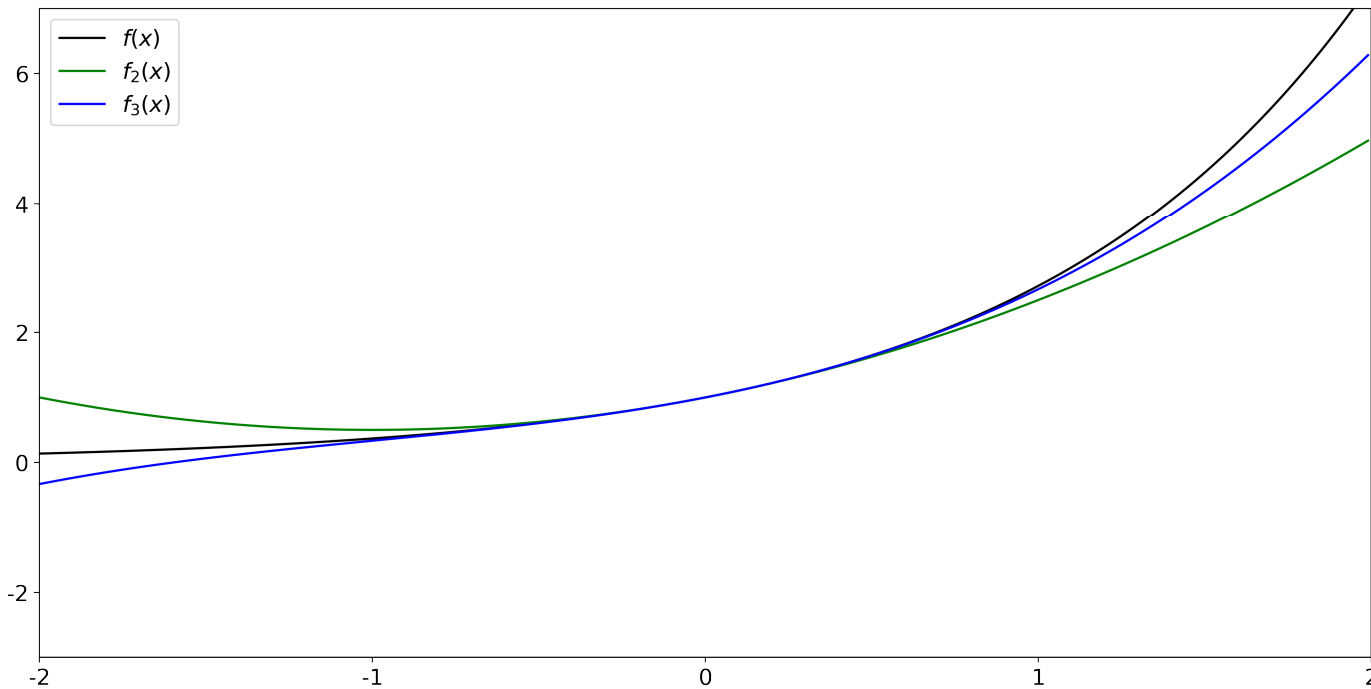
$$f_0(x) \approx 1$$

$$f_1(x) \approx 1 + x$$

# Algorithms

## Repetition – Taylor Series

$$f(x) = \sum_{i=0}^{\infty} \frac{f^{(i)}(x_0)}{i!} (x - x_0)^i$$



$$f(x) = e^x$$

$$f_0(x) \approx 1$$

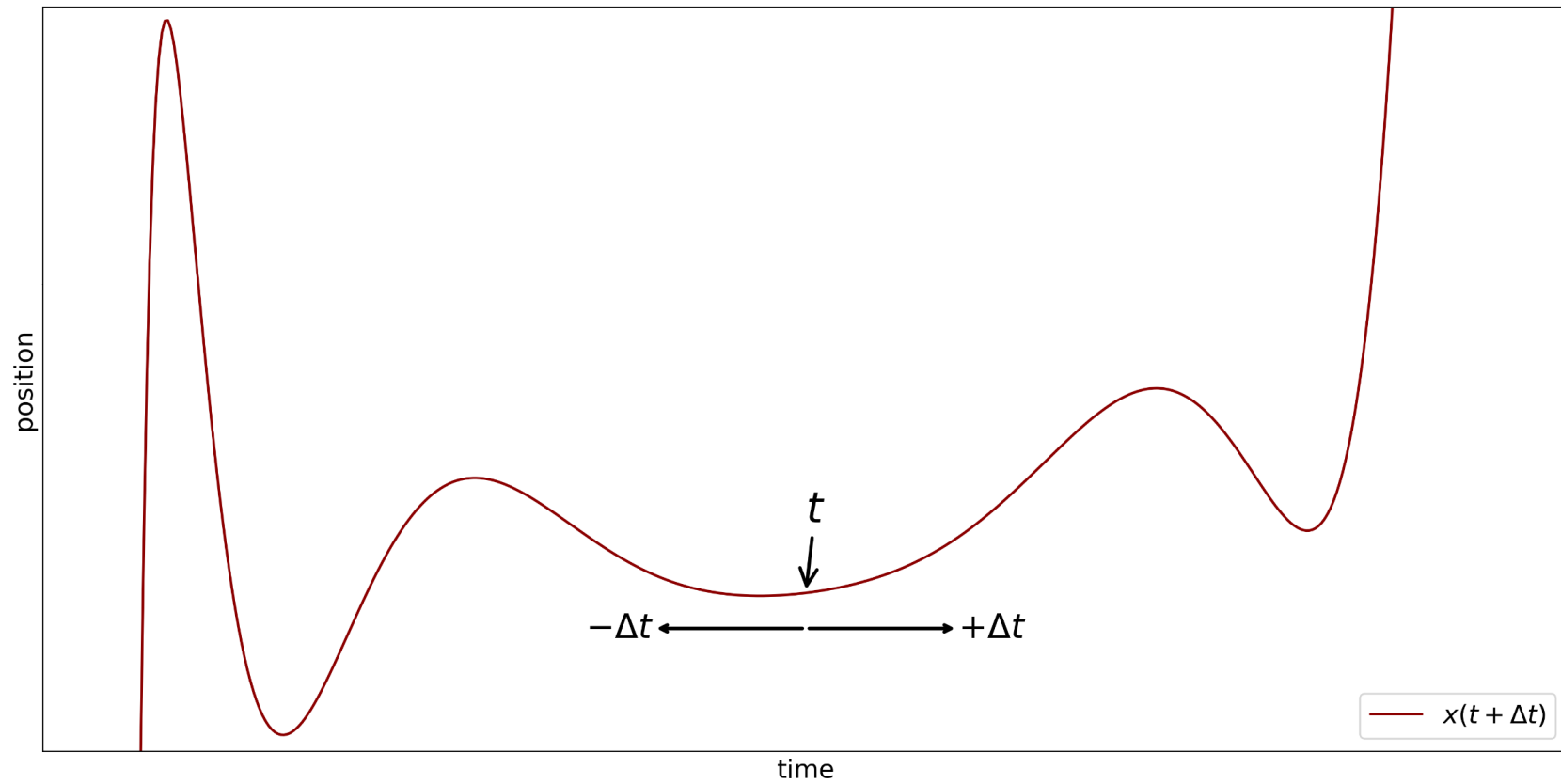
$$f_1(x) \approx 1 + x$$

$$f_2(x) \approx 1 + x + \frac{x^2}{2}$$

$$f_3(x) \approx 1 + x + \frac{x^2}{2} + \frac{x^3}{6}$$

# Algorithms

## Verlet Algorithm





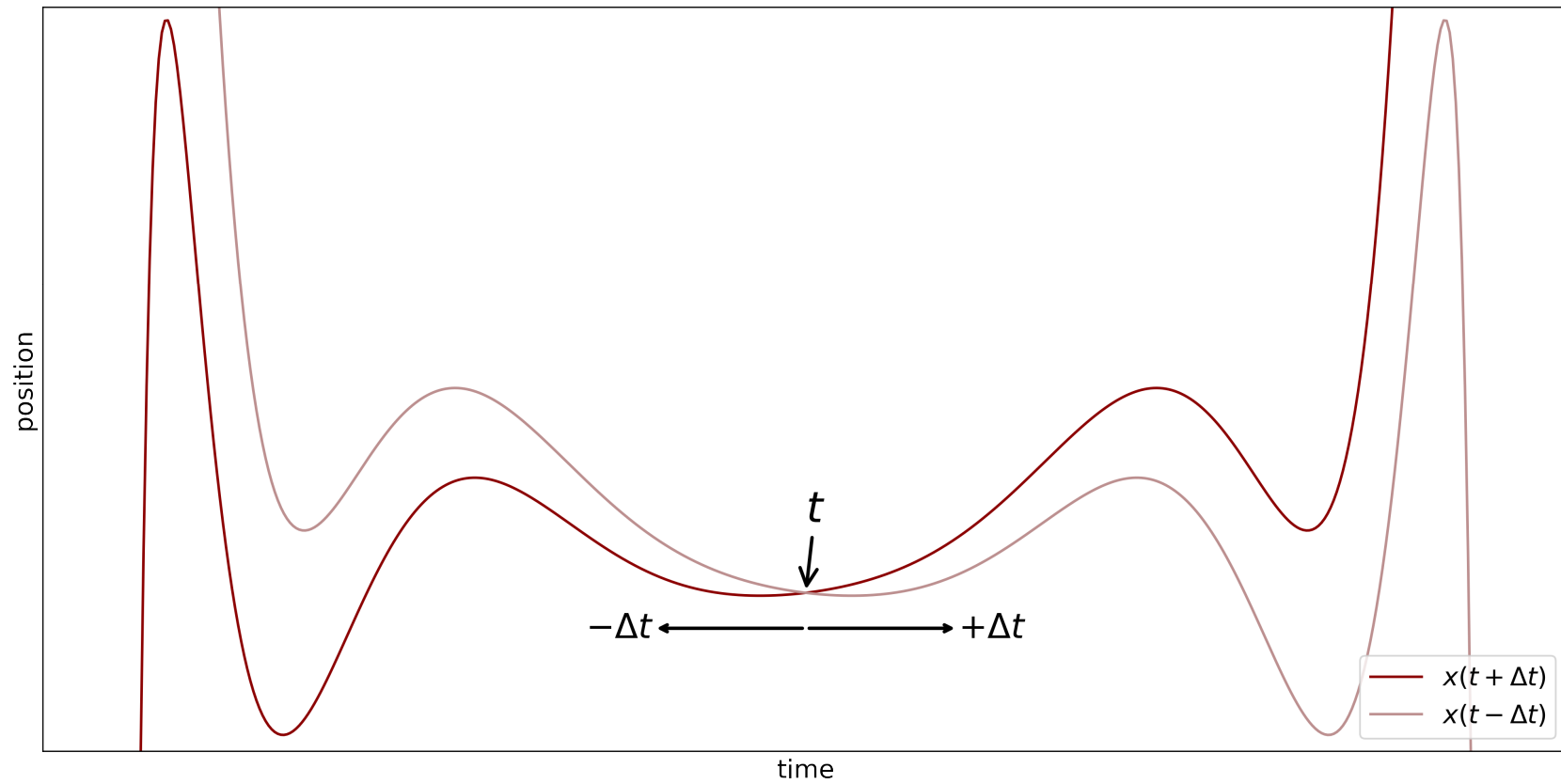
# Algorithms

## Verlet Algorithm

$$x(t + \Delta t) \approx x(t) + x'(t) \Delta t + \frac{x''(t)}{2} \Delta t^2 + \frac{x'''(t)}{6} \Delta t^3 + \mathcal{O}^4$$
$$x(t - \Delta t) \approx x(t) + x'(t)(-\Delta t) + \frac{x''(t)}{2} (-\Delta t)^2 + \frac{x'''(t)}{6} (-\Delta t)^3 + \mathcal{O}^4$$

# Algorithms

## Verlet Algorithm



# Algorithms

## Verlet Algorithm

$$x(t + \Delta t) \approx x(t) + x'(t) \Delta t + \frac{x''(t)}{2} \Delta t^2 + \frac{x'''(t)}{6} \Delta t^3 + \mathcal{O}^4$$

$$x(t - \Delta t) \approx \boxed{x(t)} + \boxed{x'(t)(-\Delta t)} + \boxed{\frac{x''(t)}{2} (\cancel{\Delta t})^2} + \boxed{\frac{x'''(t)}{6} (-\Delta t)^3} + \mathcal{O}^4$$

$$x(t - \Delta t) \approx \boxed{x(t)} - \boxed{x'(t)\Delta t} + \boxed{\frac{x''(t)}{2} \Delta t^2} - \boxed{\frac{x'''(t)}{6} \Delta t^3} + \mathcal{O}^4$$

# Algorithms

## Verlet Algorithm

$$x(t + \Delta t) \approx x(t) + x'(t)\Delta t + \frac{x''(t)}{2}\Delta t^2 + \frac{x'''(t)}{6}\Delta t^3 + \mathcal{O}^4$$
$$x(t - \Delta t) \approx x(t) - x'(t)\Delta t + \frac{x''(t)}{2}\Delta t^2 - \frac{x'''(t)}{6}\Delta t^3 + \mathcal{O}^4$$

---

$$x(t + \Delta t) + x(t - \Delta t) \approx 2x(t) + x''(t)\Delta t^2 + \mathcal{O}^4$$

# Algorithms

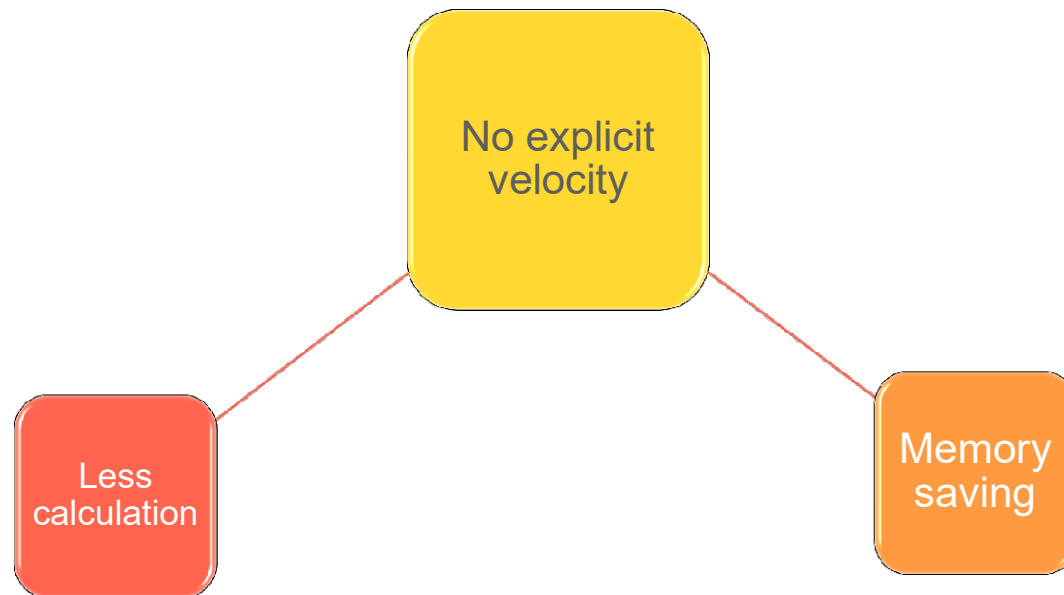
## Verlet Algorithm

Correct up to 3rd order!

$$x(t + \Delta t) \approx 2x(t) - x(t - \Delta t) + x''(t)\Delta t^2 + \mathcal{O}^4$$

# Algorithms

## Verlet Algorithm - Advantages



# 5. Coarse Grained Simulation



# Coarse Grained Simulations

## Outline

1. Simple Coarse Graining
2. Brownian Dynamics
3. Implicit Solvents

# Coarse Grained Simulations

## Important Models

- Martini
- Sirah

# Coarse Grained Simulations

## Sirah

<b>G</b> GLY 57.05 sG 6.064 Glycine	<b>A</b> ALA 71.09 sA 6.107 Alanine	<b>V</b> VAL 99.14 sV 6.002 Valine	<b>L</b> LEU 113.16 sL 6.036 Leucine	<b>I</b> ILE 113.16 sI 6.038 Isoleucine	<b>P</b> PRO 112.7 sP 6.3 Proline	<b>F</b> PHE 147.18 sF 5.91 Phenylalanine	<b>W</b> TRP 186.12 sW 5.88 Tryptophan	<b>D</b> ASP 115.09 sD 4.5 Aspartic Acid 2.98	<b>K</b> LYS 128.17 sK 9.47 Lysine 10.4	<b>R</b> ARG 173.4 sR 10.76 Arginine 12														
<b>C</b> CYS 103.15 sC 5.02 9.1-9.5 Cysteine	<b>M</b> MET 131.19 sM 5.74 Methionine	<b>S</b> SER 87.08 sS 5.68 Serine	<b>T</b> THR 101.11 sT 5.60 Threonine	<b>N</b> ASN 114.11 sN 5.41 Asparagine	<b>Q</b> GLN 128.14 sQ 5.65 Glutamine	<b>H</b> HIE 137.14 sHe 7.64 6.2 Histidine	<b>Y</b> TYR 163.18 sY 5.63 9.7 Tyrosine	<b>E</b> GLU 129.12 sE 3.08 4.6 Glutamic Acid	<table border="1"> <tr> <td>3-letters Code</td> <td>Molecular Weight (dalton)</td> </tr> <tr> <td>1-letter Code</td> <td>pI (at 25°C)</td> </tr> <tr> <td>SIRAH Code</td> <td>pK<sub>a</sub> (side-chain)</td> </tr> <tr> <td>C</td> <td>Residue Name</td> </tr> <tr> <td>C</td> <td>Atomistic Representation</td> </tr> <tr> <td>C</td> <td>SIRAH Representation</td> </tr> <tr> <td>C</td> <td>Bead Name</td> </tr> </table> <p>pK<sub>a</sub>: C. Tanford, Adv. Prot. Chem., 17(1962)69-165 pI: The Merck Index, Merck &amp; Co. Inc., Rahway, N.J., 11(1989); CRC Handbook of Chem. &amp; Phys., Cleveland, Ohio, 58(1977)</p>		3-letters Code	Molecular Weight (dalton)	1-letter Code	pI (at 25°C)	SIRAH Code	pK <sub>a</sub> (side-chain)	C	Residue Name	C	Atomistic Representation	C	SIRAH Representation	C	Bead Name
3-letters Code	Molecular Weight (dalton)																							
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C	Residue Name																							
C	Atomistic Representation																							
C	SIRAH Representation																							
C	Bead Name																							
<b>A</b> ADE 331.2 DAX Adenine	<b>G</b> GUA 347.2 DGX Guanine	<b>T</b> THY 322.2 DTX Thymine	<b>C</b> CYT 307.2 DCX Cytosine	<b>Na+</b> 22.989 NaW Sodium ion	<b>K+</b> 39.102 KW Potassium ion	<b>Cl-</b> 35.453 CIW Chloride ion	<b>WT4</b> Water model																	

The SIRAH Force Field  
www.sirahff.com



# Coarse Grained Simulations

## Brownian Dynamics

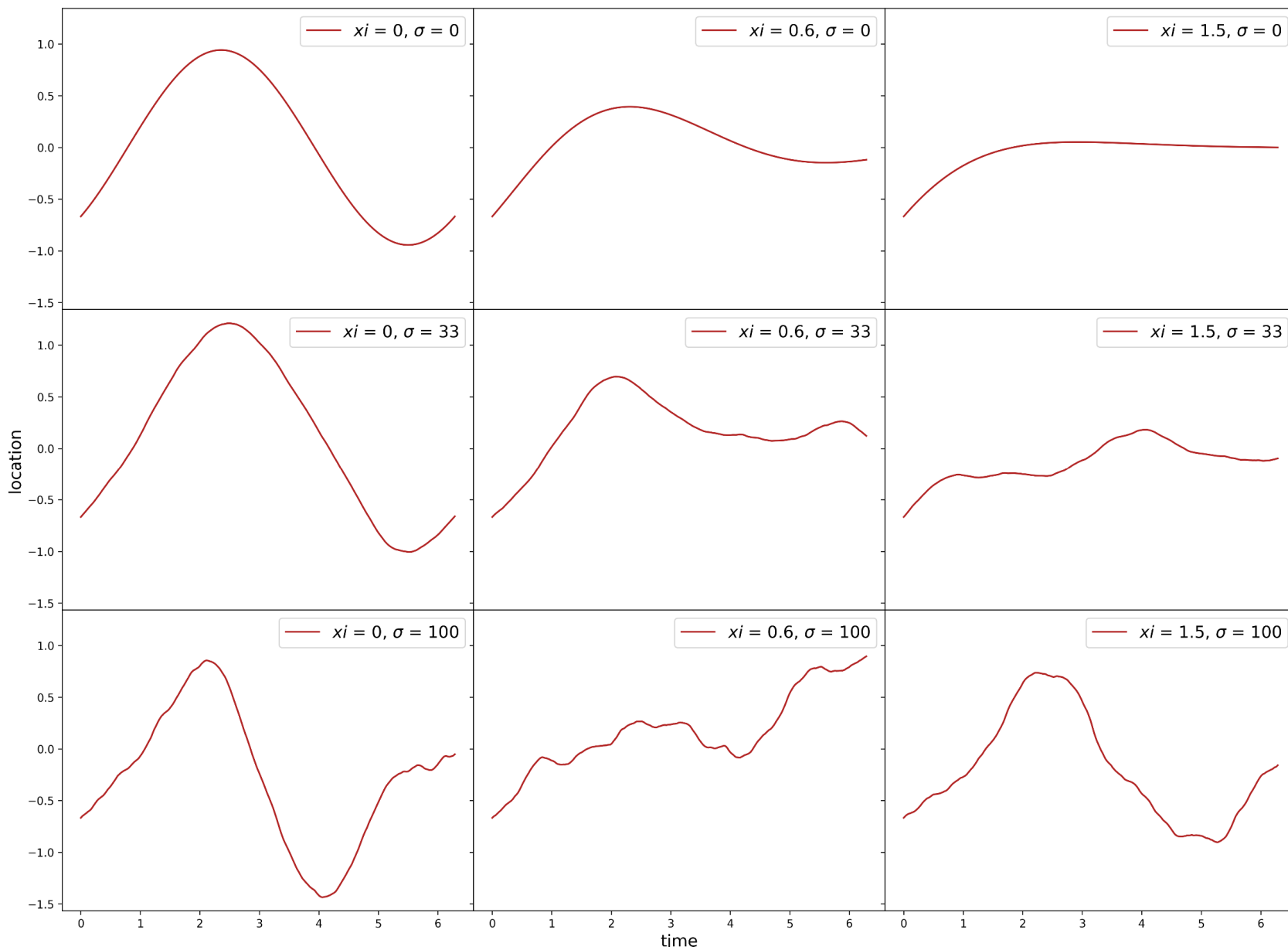
$$m\dot{v} = -\nabla V - \xi v(t) + \sigma\eta(t)$$

- $\xi$  : Stokes friction
- $\sigma$  : Random Force Amplitude
- $\eta(t)$ : Random Force

# Coarse Grained Simulations

## Brownian Dynamics

$$m\dot{v} = -\nabla V - \xi v(t) + \sigma\eta(t)$$



# Coarse Grained Simulations

## Implicit Solvents

$$\Delta G_{solv} = \sum_i \sigma_i ASA_i$$

- $\sigma_i$  : Free energy interaction - „Surface Tension“
- $ASA_i$  : Accessible Solvent Area

# 6. Recipe



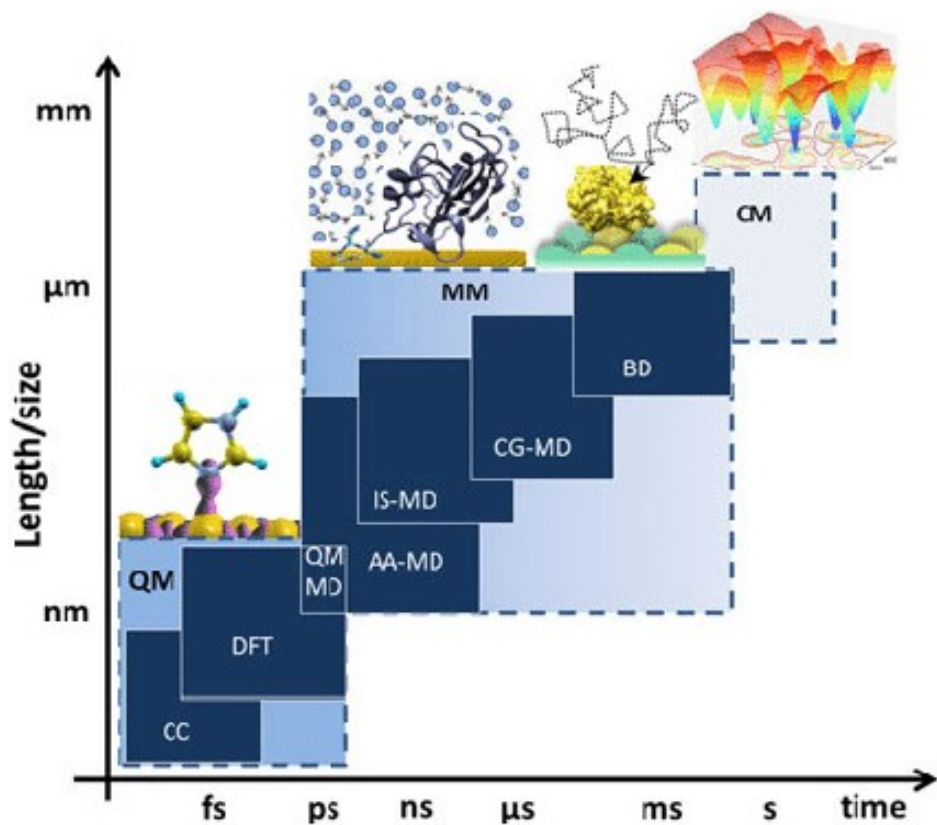
# Recipe

## Overview

1. Making Decisions
2. Data preparation
3. Minimization
4. Equilibration
5. Simulation

# Recipe

## 1. Which model?



Tunneling protons?

Chemical reactions?

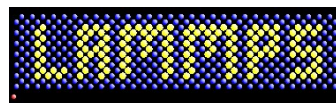
# Recipe

## 1. Which software?



**AMBER MD**

**CHARMM**  
Chemistry at HARvard Macromolecular Mechanics



**NAMD**  
Scalable Molecular Dynamics

# Recipe

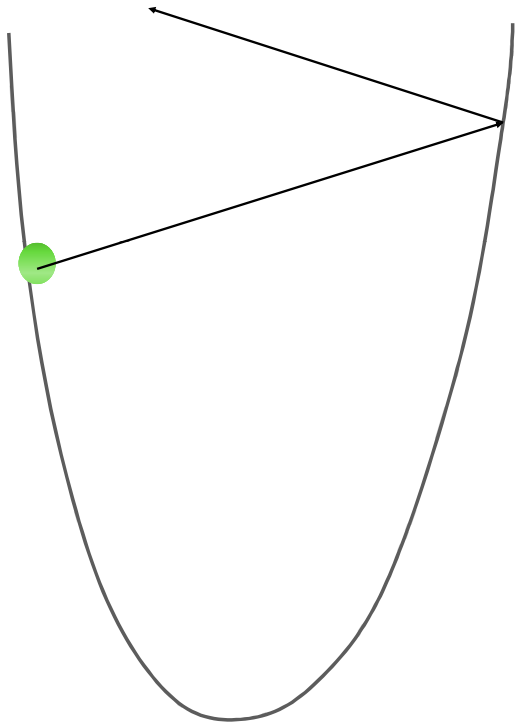
## 2. Data preparation

The screenshot shows the RCSB PDB website homepage. At the top, there is a navigation bar with links for Deposit, Search, Visualize, Analyze, Download, Learn, About, Documentation, Careers, and COVID-19. A search bar is prominently displayed with the text "Enter search term(s), Entry ID(s), or sequence". Below the search bar, there are statistics: "211,103 Structures from the PDB" and "1,068,577 Computed Structure Models (CSM)". A sidebar on the left contains navigation options: Welcome, Deposit, Search, Visualize, Analyze, Download, and Learn. The main content area features a welcome message, a list of data sources (Experimentally-determined 3D structures and Computed Structure Models), and a section for "October Molecule of the Month" featuring the RSV Fusion Glycoprotein. A banner at the bottom promotes "Explore NEW Features" and "PDB-101 Training Resources".

- .pdb file clean?
- add water
- add ions

# Recipe

## 3. Minimization



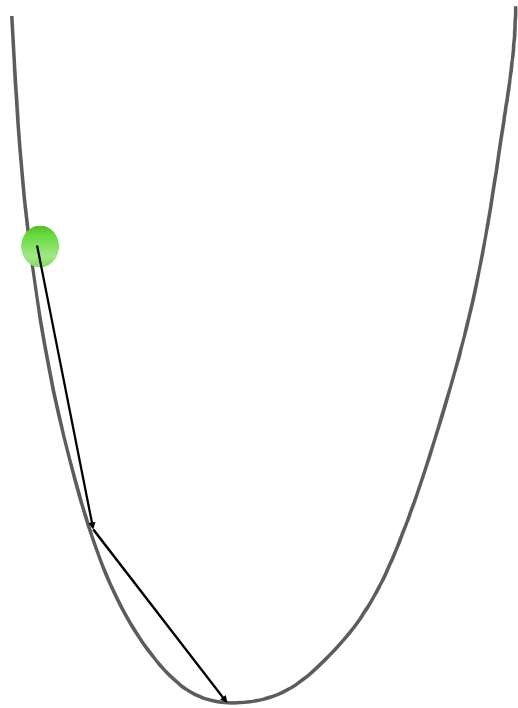
$$x''(t)\Delta t^2$$



$\nabla V = x''$  too big

# Recipe

## 3. Minimization



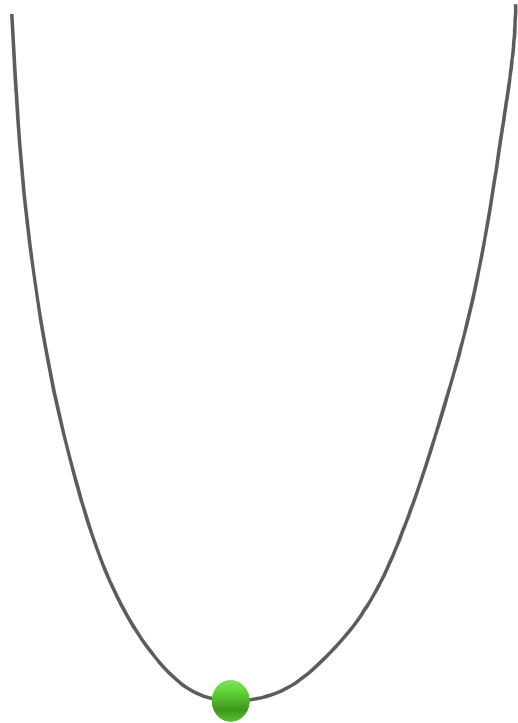
$$x''(t)\Delta t^2$$



$\Delta t$  very small

# Recipe

## 4. Equilibration



$$T = ?$$

# Recipe

## 5. Simulation

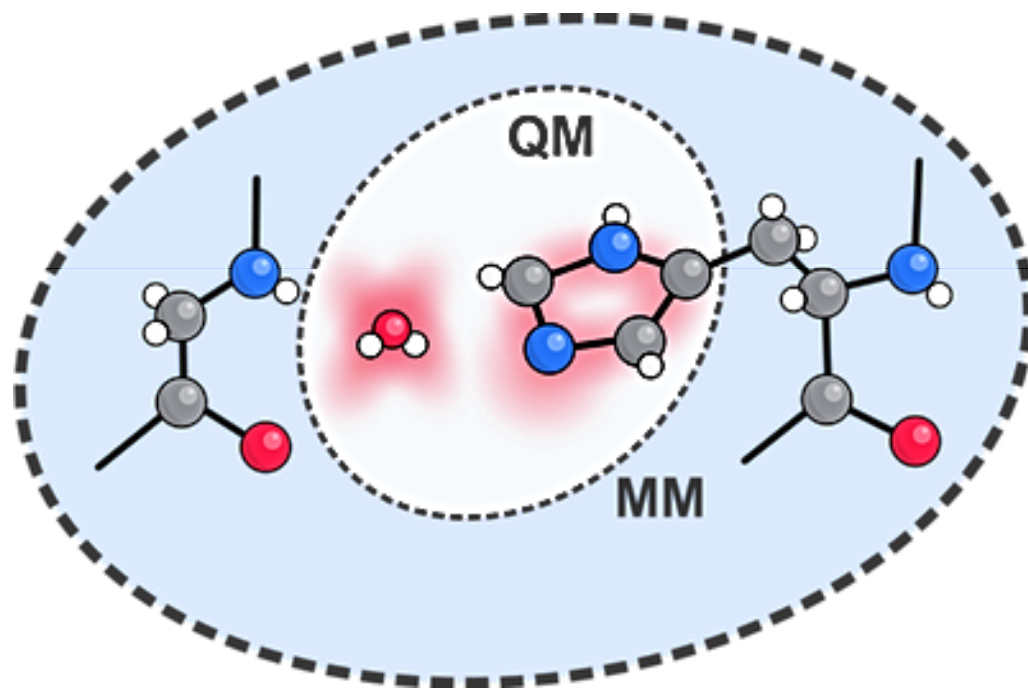




# 7. Further Studying and Possibilities

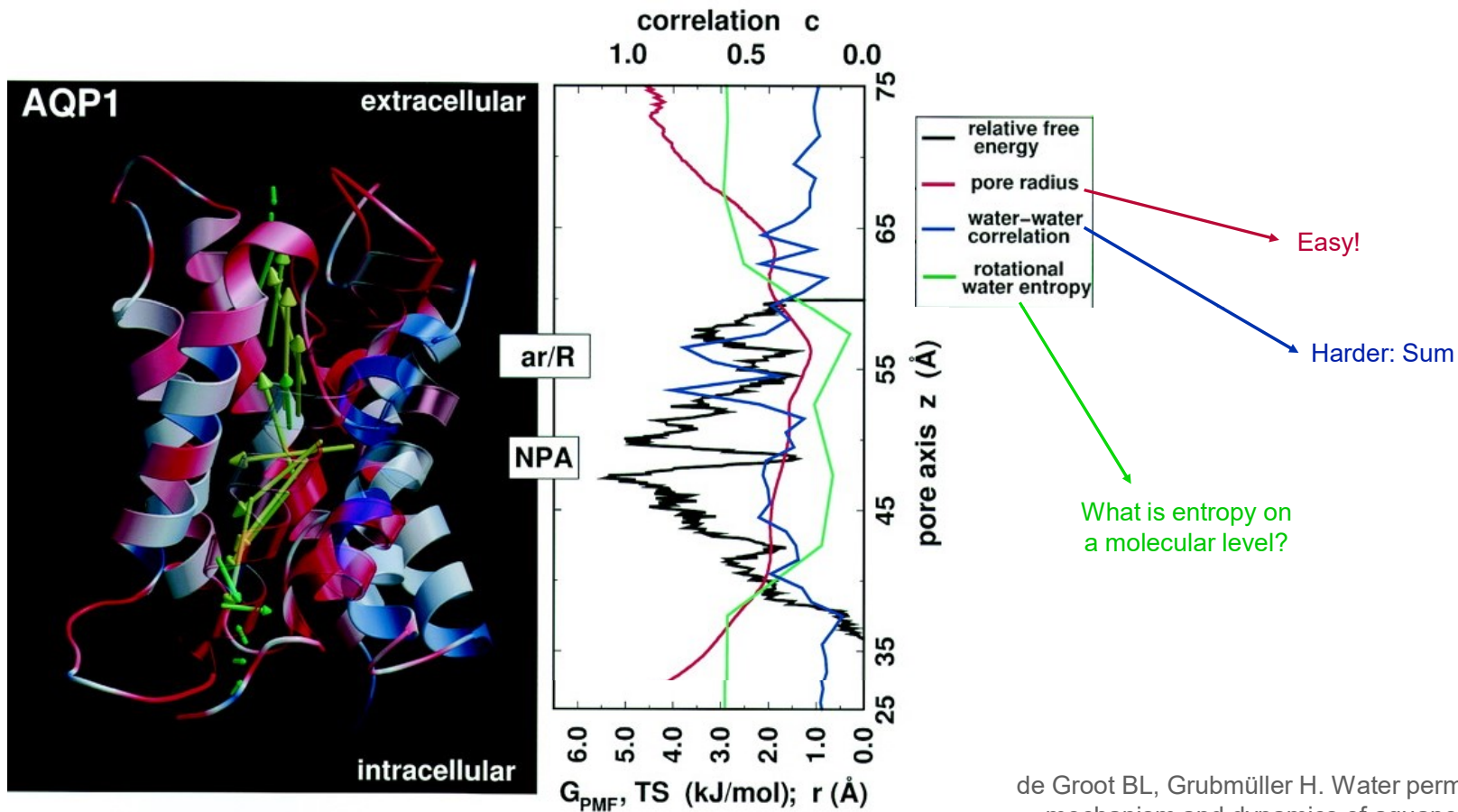
# Further Studying

QM / MM



# Further Studying

## How do we extract information from Simulations?



de Groot BL, Grubmüller H. Water permeation across biological membranes: mechanism and dynamics of aquaporin-1 and GlpF. *Science*. 2001 Dec 14;294(5550):2353-7. doi: 10.1126/science.1066115. PMID: 11743202.

# Further Studying

How do we manage other parameters?

- Thermostats / Barostats
- Fast Electrostatics (Ewald Summation)
- NMA/PCA

# Further Studying

## Helpful Courses

- Theoretical Chemistry 1 / 2
- Numerics
- Theoretical Statistical Physics

# Possibilities

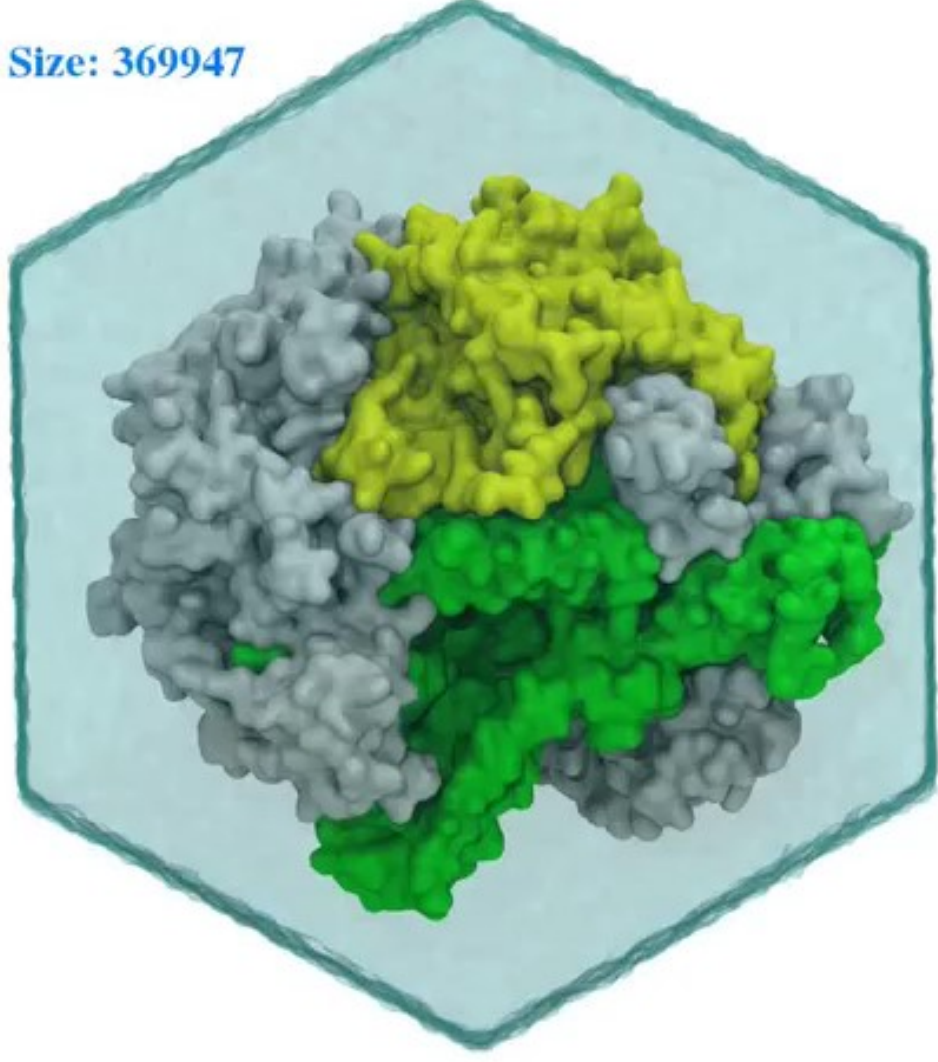
## Examples

- DNA Polymerase
- Cytoplasm
- Enzyme Catalysis

# Possibilities

## DNA Polymerase

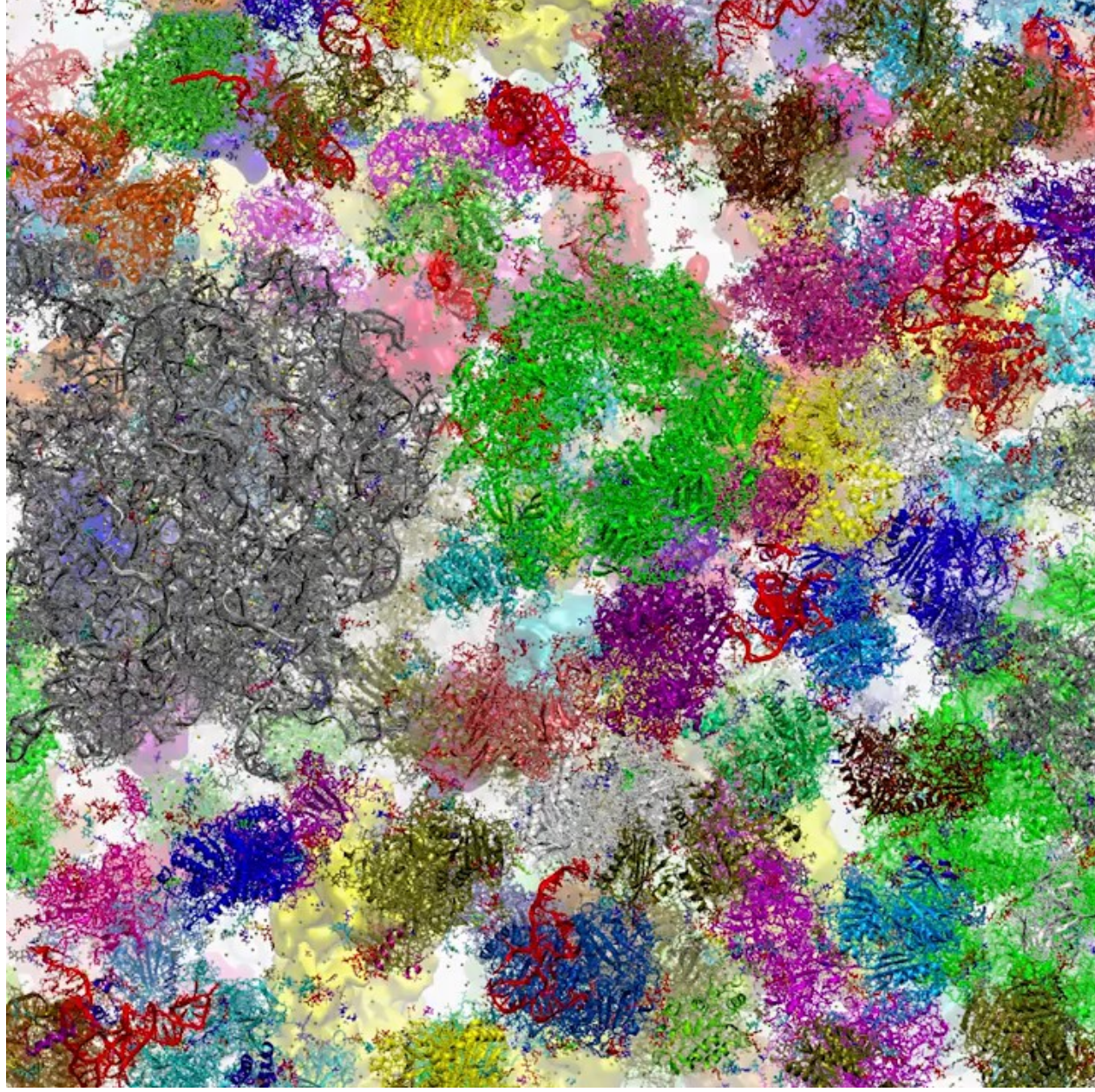
System Size: 369947





# Possibilities

## Cytoplasm





# Possibilities

## Citrate Synthase

COMMUNICATION

www.rsc.org/chemcomm | ChemComm

### High-level QM/MM modelling predicts an arginine as the acid in the condensation reaction catalysed by citrate synthase†

Marc W. van der Kamp,<sup>a</sup> Francesca Perruccio<sup>ab</sup> and Adrian J. Mulholland<sup>\*,a</sup>

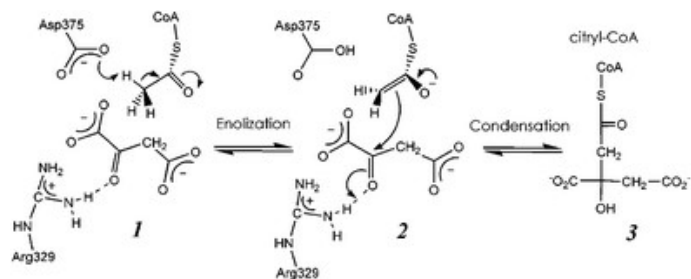
Received (in Cambridge, UK) 21st January 2008, Accepted 25th February 2008

First published as an Advance Article on the web 11th March 2008

DOI: 10.1039/b800496j

High-level *ab initio* quantum mechanical/molecular mechanical (QM/MM) modelling of citryl-CoA formation in citrate synthase reveals that an arginine residue acts as the proton donor; this proposed new mechanism helps to explain how chemical and large scale conformational changes are coupled in this paradiatomic enzyme.

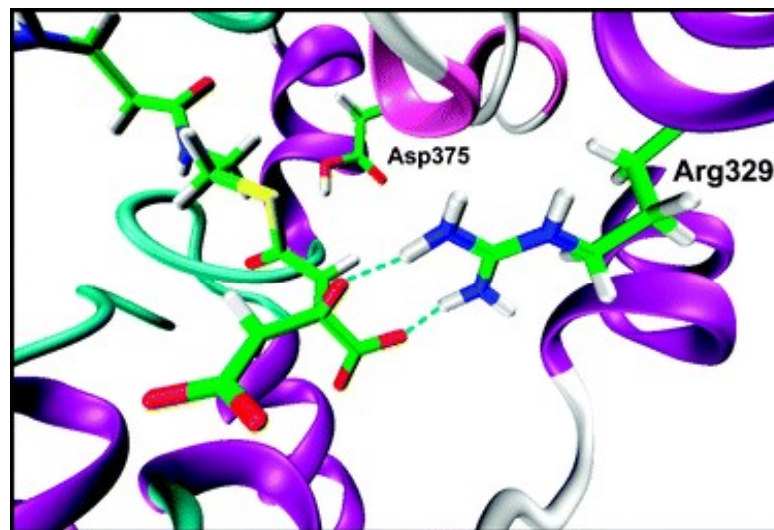
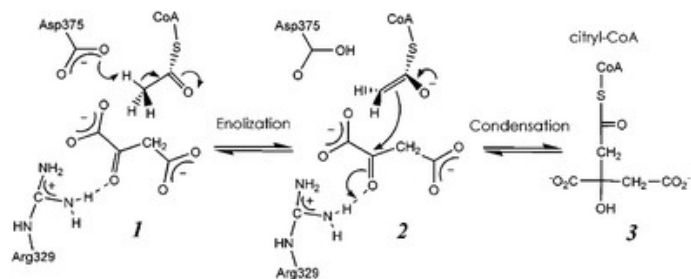
Here, we report the first modelling of the condensation reaction in CS, using high level *ab initio* QM/MM methods. The calculated potential energy profile shows that Arg329 can act as the proton donor, leading to a stable citryl-CoA intermediate. After proton abstraction from acetyl-CoA, carbon-carbon bond formation starts first but is concerted with



Van der Kamp, M. W., Perruccio, F., and Mulholland, A. J. (2008) High-level QM/MM modelling predicts an arginine as the acid in the condensation reaction catalysed by citrate synthase Chem. Commun. 1874– 1876

# Possibilities

## Citrate Synthase



Van der Kamp, M. W., Perruccio, F., and Mulholland, A. J. (2008) High-level QM/MM modelling predicts an arginine as the acid in the condensation reaction catalysed by citrate synthase Chem. Commun. 1874– 1876



# Takeaway



1. Scale method to problem
2. Force fields parametrize QM interactions
3. Force fields have 5 different contributions
4. Verlet is 3rd order algorithm
5. Simulations rely on fundamental physics

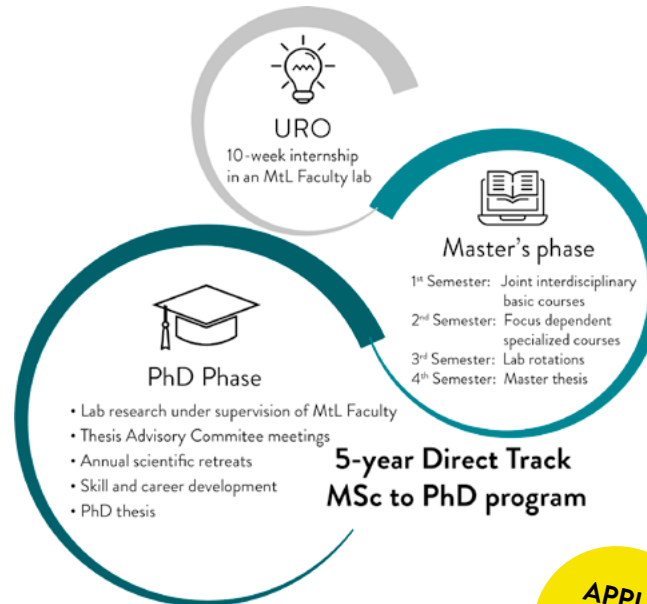
# Your Master to PhD Direct Track Program in Matter to Life

## Profile

The Max Planck Schools Matter to Life offers an innovative combined Master's/PhD program.

This international program focuses on interdisciplinary research at the crossroads of physics, chemistry and biology that pushes the boundaries of knowledge to answer the question:

„What is Life“?



**APPLY  
BY  
DEC 1<sup>st</sup>**



- ✓ Join a unique network of German universities and non-university research organizations
- ✓ Engage in cutting-edge interdisciplinary research in Matter to Life
- ✓ Receive close supervision by outstanding scientists

## Experience Matter to Life

## We offer you

- ✓ Competitive scholarships covering tuition fees and living costs
- ✓ Close supervision by outstanding scientists
- ✓ Cutting-edge interdisciplinary research in biomedical, chemical and physical sciences
- ✓ Access to first-class research infrastructures and innovative teaching formats
- ✓ Studying and working in an international and diverse environment
- ✓ Be part of the established alumni network
- ✓ Future career growth in academia or industry

## Course structure

The Master's phase includes lecture modules, lab rotations, internships, and the master thesis, thus giving you a theoretical and practical overview of the research done by our faculty. These experiences will perfectly prepare you to make an informed decision regarding the lab and project in which to carry out your PhD thesis in.

Continuous support in the form of mentoring by peers & faculty, thesis advisory committee meetings, funding for travelling to conferences and career trainings are also provided.

## Who can apply?

Candidates with a Bachelor's degree (B.Sc or B.E) or who are in their final study year in chemistry, biochemistry, physics, bioengineering or related subjects. And of course, passion for science and research!

"The program offers a truly interdisciplinary education. I am able to take classes in a variety of fields and connect with international students and faculty from different backgrounds. The professors are knowledgeable and supportive. I particularly appreciate the hands-on learning opportunities at the University and Max Planck Institute for Medical Research with top-notch facilities."

Deus Mwesigwa, 24, Matter to Life, Master Student



## Important dates

- September 1** - Start of application phase
- December 1** - Application deadline
- September 1** (following year) - Program start

## Join one of our online info sessions!

Find the dates on our website during the application phase



## Check our website for more information

Master/PhD Program

<https://mattertolife.maxplanckschools.org/program>

MtL URO Program

[mattertolife.maxplanckschools.org/uro-research-internship](https://mattertolife.maxplanckschools.org/uro-research-internship)

## Contact us

[mattertolife@maxplanckschools.de](mailto:mattertolife@maxplanckschools.de)

[uro@mtl.maxplanckschools.de](mailto:uro@mtl.maxplanckschools.de)

## Follow us on Social Media



## Undergraduate Research Opportunities

The Matter to Life school offers outstanding undergraduate students the opportunity to expand their research experience through our Undergraduate Research Opportunities (URO) program.

## Who can apply?

All motivated undergraduate students during their Bachelor studies in an MtL related field are eligible to apply!

## What the MtL URO program entails

- ✓ A 10-week hands on internship in one of the laboratories of our renowned faculty
- ✓ Learn cutting-edge scientific methods in the context of Matter to Life
- ✓ Gain insights into the Matter to Life community
- ✓ Establish your network and expand your knowledge in a highly interdisciplinary field
- ✓ Receive financial support for your travel, accommodation and living expenses during your stay

